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## NEW W WING SHAPE FOR AIRMODELS

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**Abstract:** The new W wing shape (half wing, with “a” half wingspan and “h” wingtip height) approximates the front seen parabola ideal wing by straight lines: line 1 touches parabola at the axis origin and is 25 % of “a”, line 2 is tangent of parabola at the wingtip and cuts the horizontal line at 50 % of “a”, and line 3 is tangent to parabola, cuts horizontal line at 25 % of “a” and cuts line 2 at 75 % of “a” and 50 % of “h”. Real W wing approximated very close the ideal parabolic wing. The new W wing gives more lateral and directional stability.

**Key words:** New W wing shape, Parabola lines approximation, Glider airmodel.

### 1. INTRODUCTION

An airmodel glider wing may have some different shapes: elliptical or squared, straight or cranked [1]. An explanation for the wing lift is proposed by Chattot in [2]. The perfect shape wing is elliptical (F.W. Lanchester) [3] and gives a minimum induced drag.

The wing may have winglets [4]. This idea was launched long before the flights started [3].

Discussion about the shape of the perfect wing for minimum induced drag is continued in [5-7]. We do not deal with this discussion.

The wing is attached at the top of the fuselage.

For lateral stability it was necessary to introduce dihedral – the slight upward tilt of the wings [3]. The dihedral could be replaced with parabola by optimization [8]. We shall use parabola in present calculation for establishing the new W wing shape for airmodels.

Glider wings are constructed using wood, carbon fiber, or a combination of materials to provide maximum strength. Their structure is of ribs running chordwise from leading edge to trailing edge, and longeron. The edges are made of straight sticks for easy construction, check, and repair. Resulting a need of approximation of parabola with straight lines. The present paper

deals with parabola approximation by straight lines, resulting a new W wing shape.

### 2. STREIGHT LINES APPROXIMATION OF PARABOLA

The parabola wing shape seen from the front is approximated by straight lines as in Figure 1.

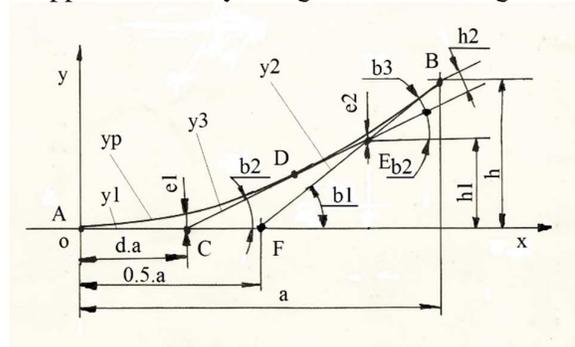


Fig. 1. The parabola,  $y_p$ , approximated by straight lines  $y_1$ ,  $y_2$ , and  $y_3$ .

Parabola,  $y_p$ , is approximated by three straight lines,  $y_1$ ,  $y_2$ , and  $y_3$ . It passes through the points:

$$A(x_A, y_A) \text{ and } B(x_B, y_B);$$

where

$$x_A = 0, y_A = 0$$

and

$$x_B = a - \text{half wingspan,} \\ y_B = h - \text{wingtip height.}$$

It had the equation

$$y_p = (h/(a^2))x^2. \quad (1)$$

The line 1,  $y_1$ , passes A(0, 0) tangents  $y_p$ , and has the equation

$$y_1 = 0, \quad (2)$$

The line 2,  $y_2$ , has the equation

$$y_2 = m_2x + n_2. \quad (3)$$

It tangents parabola,  $y_p$ , in B(a, h)

$$m_2 = (dyp/dx)_B = 2h/a. \quad (4)$$

Angle  $b_1$  is

$$b_1 = \text{arc tg } m_2 = \text{arc tg } (2h/a). \quad (5)$$

Line 2,  $y_2$ , passes through B(a, h) so

$$y_2 = h = (2h/a)a + n_2. \quad (6)$$

from where

$$n_2 = -h, \quad (7)$$

resulting the equation of  $y_2$

$$y_2 = (2h/a)x - h \quad (8)$$

Line  $y_2$  cuts ox axes so

$$y_2 = 0 = (2h/a)x - h \quad (9)$$

from where

$$x = 0.5.a. \quad (10)$$

Line 3,  $y_3$ , has the equation

$$y_3 = m_3x + n_3 \quad (11)$$

and passes through C( $x_C$ ,  $y_C$ ) where

$$x_C = d.a, y_C = 0 \quad (12)$$

where d represents a fraction of "a". Equation becomes

$$0 = m_3(d.a) + n_3 \quad (13)$$

from where

$$n_3 = - m_3(d.a). \quad (14)$$

The  $y_3$  equation becomes

$$y_3 = m_3x - m_3(d.a). \quad (15)$$

Parabola,  $y_p$ , and line 3,  $y_3$ , are cut in

$$y_p = (h/a^2)x^2 = y_3 = m_3x - m_3(d.a). \quad (16)$$

In other shape looks

$$(h/a^2)x^2 - m_3x + m_3(d.a) = 0 \quad (17)$$

like

$$ax^2 + bx + c = 0,$$

where a, b, and c are other constants than those defined before.

Considering

$$\Delta = b^2 = 4ac$$

and if

$$\Delta > 1, x_{1,2} = (-b \pm \Delta^{1/2})$$

$$\Delta = 0, x_1 = x_2 = -b/(2a)$$

$$\Delta < 1, \text{ roots are not real.}$$

In this case they cut themselves in a single point, 13 tangents  $y_p$ , so

$$\Delta = (-m_3)^2 - 4 (h/(a^2))m_3(d.a) = 0$$

or

$$m_3(m_3 - 4(h/(a^2))(d.a)) = 0 \quad (18)$$

resulting

$$m_{3,1} = 0 \quad (19)$$

corresponding with  $m_1$  of  $y_1$ , and

$$m_{3,2} = m_3 = 4(h/a)d. \quad (20)$$

Equation of  $y_3$  becomes

$$y_3 = 4(h/a)d.x - 4hd^2 \quad (21)$$

Line 2,  $y_2$ , cuts  $y_3$  in  $E(x_E, y_E)$

$$y_2 = 2(h/a)x - h = y_3 = 4(h/a)d.x - 4h.d^2 \quad (23)$$

resulting

$$x_E = a(0.5 + d) \text{ and } y_E = h_1 = 2hd. \quad (24)$$

The horizontal distances ( $x$ ) are connected to “ $a$ ” and vertical distances ( $y$ ) to “ $h$ ” only.

Deviations  $e_1$  and respectively  $e_2$  from the parabola,  $y_p$ , of  $C$  and respectively  $E$  points, Figure 1, are

$$e_1 = (y_p)_{x_C} - h.d^2 \quad (25)$$

$$e_2 = (y_p)_{x_E} - (y_2)_{x_E} = h(0.25 - d + d^2). \quad (26)$$

Introducing condition of equality between  $e_1$  and  $e_2$

$$e_1 = e_2 \quad (27)$$

results

$$d = 0.25. \quad (28)$$

So

$$e_1 = e_2 = 0.0625h. \quad (29)$$

Values  $AC$ ,  $CE$ ,  $EB$ , and  $ACEB$

$$AC = x_C - x_A = d.a = 0.25a \quad (30)$$

$$CE = 0.5(a^2 + h^2)^{1/2} \quad (31)$$

$$EB = 0.25(a^2 + 4h^2)^{1/2} \quad (32)$$

$$ACEB = 0.25(a + 2(a^2 + b^2)^{1/2} + (a^2 + 4b^2)^{1/2}) \quad (33)$$

The distances (not  $x$  or  $y$ ) are connected to  $a$ ,  $h$ , and  $d$ .

Let us consider  $a = 100$  mm and  $h = 20$  mm, resulting a wing as in Figure 2, with values:

$$d = 25 \text{ mm}$$

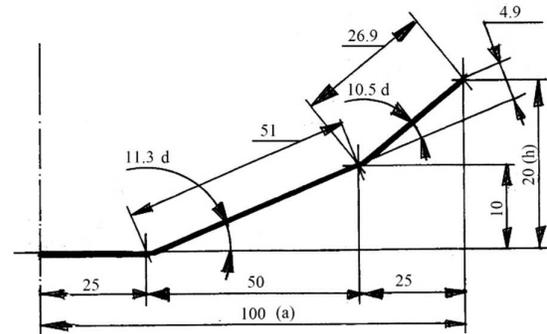


Fig. 2. Approximation of parabola with straight lines as present calculation having  $a = 100$  mm and  $b = 20$  mm.

$$h_1 = 10 \text{ mm}, h_2 = 4.90 \text{ mm}.$$

$$b_1 = 21.80^\circ, b_2 = 11.31^\circ, b_3 = 10.49^\circ$$

$$e_1 = e_2 = 1.25 \text{ mm};$$

$$ACEB/a = 1.0292.$$

In the case of Figure 2 “approximation of parabola with straight lines as present calculations, having  $a = 100$  mm and  $h = 20$  mm” is seen: horizontal part is 25 %, first tilt is at 50 %, and second tilt is at 25 % of “ $a$ ”. The first tilt is at 0 % and the second tilt is at 50 % of “ $h$ ”. The deviation from the parabola in tilting places is equal in both places to 6.25 % of “ $h$ ”, which is very low. The approximation by straight lines is very close to the parabola.

### 3. REAL WING CONSTRUCTION

A new **W wing shape** using these considerations was designed and built, Figure 3.

It is seen the wing shape is almost parabola. The wingspan ( $2a$ ) is 2192 mm and flying speed is 5.5 m/s. Its weight is 654 g.

The real wing of Figure 3 is not exactly as that theoretical of Figure 2, considering the proper scale. The real one has horizontal part 2.2 % greater, first tilt to second tilt equal to, and from the second tilt to wing tip shorter than the theoretical one, for building considerations. These deviations of real wing to the theoretical

