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DETERMINATION OF THE BRAKING CHARACTERISTICS IN CASE OF THE VARIATION DEPENDING ON THE TEMPERATURE OF THE MATERIAL PROPERTIES OF THE FRICTION COUPLING OF THE DISC BRAKE OF RAILWAY VEHICLES

Liviu Sevastian BOCÎI, Jacob Javier VÁSQUEZ SANJUÁN

Abstract: The safety of classic and high-speed rail vehicles depends on the mode of operation and the characteristics of their braking systems. Braking of railway vehicles (especially stopping braking) can be performed using brakes of the same system (for example, shoe brake or disc brake of the mechanical braking system) or by combining brakes of several systems (disc brake - mechanical braking system), mechanical, electromagnetic rail brake or resistive or regenerative electric brake - electric braking system). During stop braking, the friction elements of the main brake - the disc brake - reach quite high temperatures (especially when braking at high speeds: $V > 160$ km/h) which leads to the alteration of the physical- chemical and mechanical properties of the materials of these elements.

This work presents the braking characteristics of railway vehicles (friction coefficient, braking space and deceleration when braking) in case of variation of the physical properties (specific heat and thermal conductivity) of the materials of the friction coupling elements of the railway. disc brake (friction pad and brake disc) as a function of temperature.

Key words: Physical properties, Mechanical braking system, Pad, Brake disk, Brake stopping.

1. INTRODUCTION

The determination method of the brake characteristics and the brake disk friction surface temperature, proposed by Hasselgruber [11-12], shows a series of deficiencies, such: physical properties of the friction coupling material elements (density, specific heat, thermal conductivity) were considered constant with temperature variation, fact which was not confirmed by the experimental trials done later on [2].

Taking into account these deficiencies, the author of this work considers the variation with temperature of the specific heat c_d , c_g and of the thermal conductivity λ_d and λ_g , of the disk and of the friction pad (*composite material*). Also, we consider a straight-line variation of the speed with period of braking at a brake stopping.

At the brake characteristics determination at a brake stopping with disk brake help, in this

work were taken into account the next hypothesis:

- the vehicle speed varies straight-line depending on time at a brake stopping;
- the physical properties (specific heat and thermal conductivity) of the friction coupling material elements vary depending on temperature;
- the optimal time of braking was considered $t_b = 60$ s, taking into account the brake spaces and decelerations admitted;
- the neglecting of the influence of the radiation and heat convection at brake stopping due to the small time of this;
- the densities of the materials from which are made the friction coupling elements were considered constant with temperature;
- the friction coefficient between the brake disk and friction pad (set) determined by the Karwatsky, [13], formula helping, for three pressure forces of the friction pad (set) on the disk: $F_{b1} = 20$ KN, $F_{b2} = 45$ KN, $F_{b3} = 50$

$$b_k = \sum_{i=1}^n c d_i \cdot T_i^{k-1} \text{ sau } b_k = \sum_{i=1}^n c g_i \cdot T_i^{k-1}, \quad k = 1, \dots, m+1$$

Table 1 The approximation polynomial coefficients for specific heats

The polynomial approximation coefficients	$c_d = f(T)$ ($m = 9$)	$c_g = f(T)$ ($m = 9$)
c_1	533,988	$1,467 \cdot 10^3$
c_2	0,78761	-0,60434
c_3	-0,00338	-0,03794
c_4	$5,736 \cdot 10^{-5}$	0,00117
c_5	$-9,814 \cdot 10^{-7}$	$-1,787 \cdot 10^{-5}$
c_6	$9,324 \cdot 10^{-9}$	$1,495 \cdot 10^{-7}$
c_7	$-5,065 \cdot 10^{-11}$	$-7,200 \cdot 10^{-10}$
c_8	$1,574 \cdot 10^{-13}$	$1,984 \cdot 10^{-12}$
c_9	0	$-2,90643415749037 \cdot 10^{-15}$
c_{10}	0	0

For a quick and exact solving of the linear system (2) it was used the utilitarian Mathcad.

By means of the coefficients which were determined and shown in table 1 we can write the approximation polynomial of the $c_d = f(T)$ and $c_g = f(T)$ functions.

$$c d_i = c_1 + c_2 \cdot T_i + c_3 \cdot T_i^2 + \dots + c_{10} \cdot T_i^9$$

$$c g_i = c_1 + c_2 \cdot T_i + c_3 \cdot T_i^2 + \dots + c_{10} \cdot T_i^9$$

In figures 1 and 2, there are represented the variation of the specific heat for the friction coupling material elements, for the range of temperature (0 - 350)° C, by means of cubic spline interpolation functions.

Analyzing the following figures we can observe a complete different variation with temperature of the specific heat for the two friction coupling materials (increasing carriage for the specific heat with temperature for the brake disk and a decreasing carriage for the specific heat with temperature for the friction pad material).

These variations of the specific heat have a large influence upon thermal regime of the friction surface of the friction coupling elements of the disk brake.

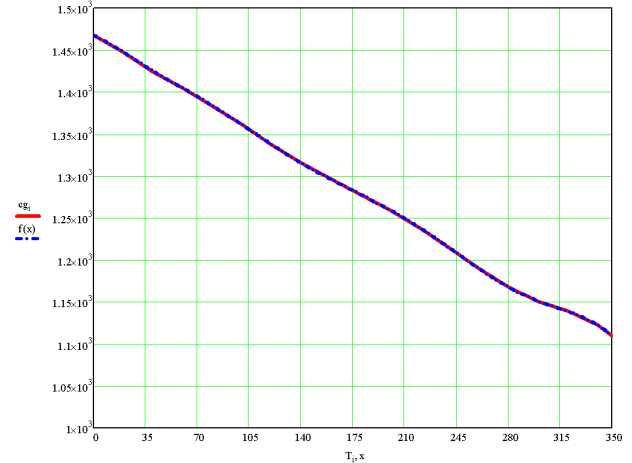


Figure 1. The variation of the friction pad material specific heat vs. the temperature.

Thermal conductivity (λ) of the gray irons is dependent both on metallic mass structure and on temperature. An important influence on gray iron thermal conductivity is given by the conductivity of the main structural constituents (pearlite, ferrite, graphite) and the aspects in which the graphite is in the structure (gray iron with flaked graphite has a larger thermal conductivity than gray iron with module graphite). on the gray iron thermal conductivity actuates even more the carbon content and the addition agent.

Thus, the increasing of the carbon content can produce a decreasing or an increasing of the thermal conductivity depending on the constituents, which of them are in advantage by this increasing.

For example, the increasing of the pearlite amount and cementite amount produces a decreasing of thermal conductivity, while the increasing of the graphite amount determines an increasing of the thermal conductivity.

The addition elements (silicon, mangan, aluminum, chrome, copper, nickel, tungsten, molybdenum, vanadium) have a different influence on thermal conductivity on determined temperature ranges [15] (silicon, mangan, aluminum, copper and nickel lead to a decreasing of the thermal conductivity).

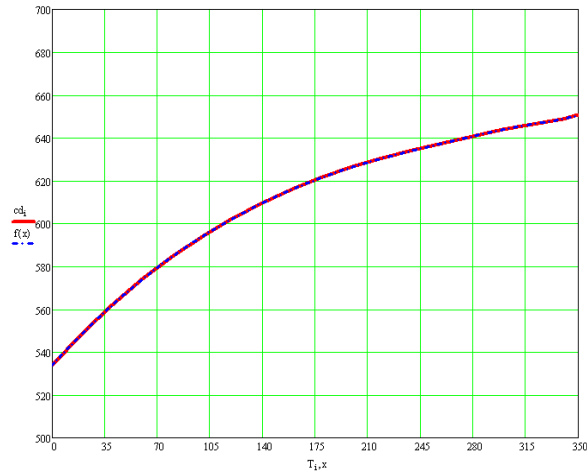


Figure 2. The variation of the disk brake specific heat vs. the temperature.

The thermal conductivity of the friction pad material (*composite material*) is framed at variation with temperature in the dispersion range: $\lambda_g = (0,16282 - 1,01181) \text{ W/m}\cdot\text{°C}$.

Using the thermal conductivity of the friction coupling material elements, for different temperatures, which are shown in specialty literature [15-19], were determined the approximation polynomial coefficients for the functions $\lambda_d = f(T)$ and $\lambda_g = f(T)$, using the smallest squares method.

The determination of the approximation polynomial coefficients is done using the next linear algebraic system (2), where:

$$S_k = \sum_{i=1}^n T_i^{k-1}, \quad k = 1, 2, \dots, 2m+1$$

$$b_k = \sum_{i=1}^n \lambda_{d_i} \cdot T_i^{k-1} \quad \text{or} \quad b_k = \sum_{i=1}^n \lambda_{g_i} \cdot T_i^{k-1} \quad k = 1, 2, \dots, m+1$$

$m = \text{approximation polynomial power}$

By helping Mathcad computer program, were determined the values of the approximation polynomial coefficients, which are shown in table 2:

Table 2 The approximation polynomial coefficients for thermal conductivity

The approximation polynomial coefficients	$\lambda_d = f(T)$ ($m = 8$)	$\lambda_g = f(T)$ ($m = 9$)
c_1	49,988	0,88662
c_2	0,19636	0,00434
c_3	- 0,00301	-2,533·10 ⁻⁵
c_4	1,496·10 ⁻⁵	-5,661·10 ⁻⁷

c_5	- 1,006·10 ⁻⁷	9,630·10 ⁻⁹
c_6	6,129·10 ⁻¹⁰	-6,692·10 ⁻¹¹
c_7	-1,773·10 ⁻¹²	2,403·10 ⁻¹³
c_8	2,086·10 ⁻¹⁵	0
c_9	0	0
c_{10}	0	0

In figures 3 and 4 there are shown the thermal conductivity variation for friction coupling material elements for the noted temperature ranges, using the cubic spline interpolation functions.

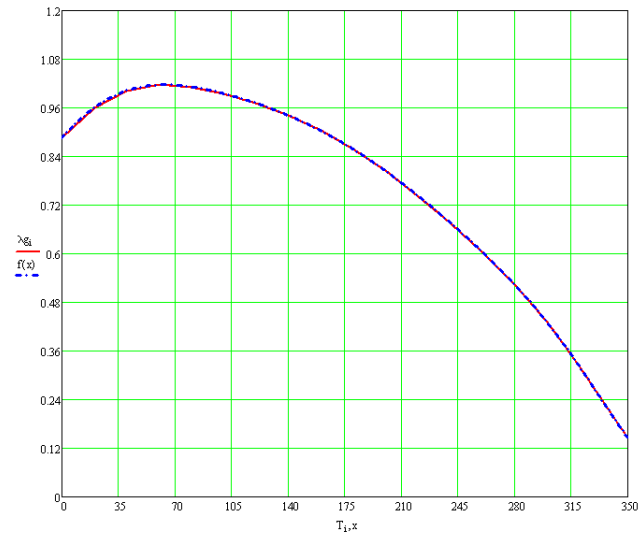


Figure 3. The variation of the friction pad thermal conductivity vs. the temperature

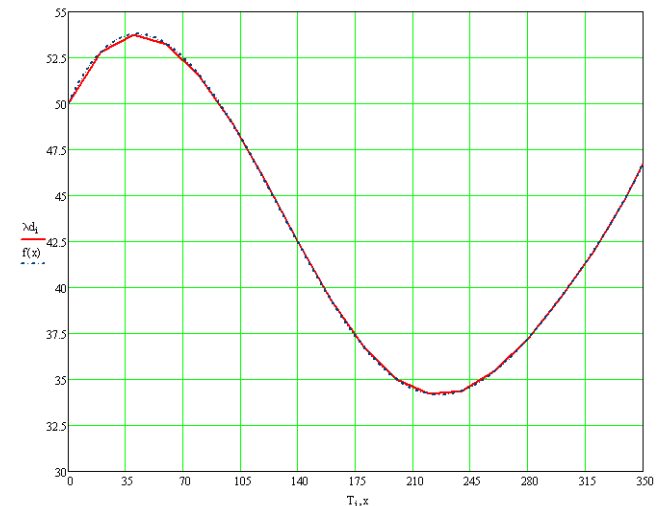


Figure 4. The variation of the brake disk material thermal conductivity vs. the temperature.

We can observe that there are different variations of the thermal conductivity depending on temperature, and this can lead at a variation of the material factor (f_m) depending on

temperature with influences on thermal regime of the friction surfaces of the brake disk elements.

3. RESULTS AND DISCUSSIONS

The specific head and the thermal conductivity of the friction coupling material elements vary many with the temperature; this thing influences the brake characteristics and the value of the average temperature of the friction surfaces of the brake disk and of the friction pad.

Material factor f_m [10-12] which is considered constant with temperature it was reconsidered, keeping in to account of the modification of the specific heat (c) and of the thermal conductivity (λ) depending on temperature. Thus, the material factor f_m is not any longer constant with temperature but depended on it. The calculation relation of this is next:

$$f_m(T) = \frac{2}{1 + \frac{\sqrt{\rho_g \cdot c_g(T) \cdot \lambda_g(T)}}{\sqrt{\rho_d \cdot c_d(T) \cdot \lambda_d(T)}}} \quad (3)$$

where: $c_g(T)$, $c_d(T)$ are the variation laws of the friction pad material (*composite*) specific heat and of the brake disk depending on temperature;

$\lambda_g(T)$, $\lambda_d(T)$ are the variation laws of the friction pad material (*composite*) thermal conductivity and of the brake disk depending on temperature;

ρ_g , ρ_d are the densities of the friction pad material (*composite*) and of the brake disk consider constant depending on temperature variation.

Using relation (3) and the variation laws of the physical properties depending on temperature were determined de values for the material factor, for the temperature range (0 - 350)° C, shown in table 3, and in diagram in figure 5 it was represented the variation of this factor depending on temperature.

Table 3. The material factor values

Temperature [°C]	Material factor f_m [dimensionless]
0	1,7675546671
20	1,7692311740

40	1,7707183180
60	1,7718700944
80	1,7724014406
100	1,7721022945
120	1,7709978086
140	1,7695004282
160	1,7684867293
180	1,7692154797
200	1,7730164523
220	1,7807997443
240	1,7926605546
260	1,8079457788
280	1,8258685995
300	1,8463290917
320	1,8704250923
340	1,8999820460
350	1,9168198656

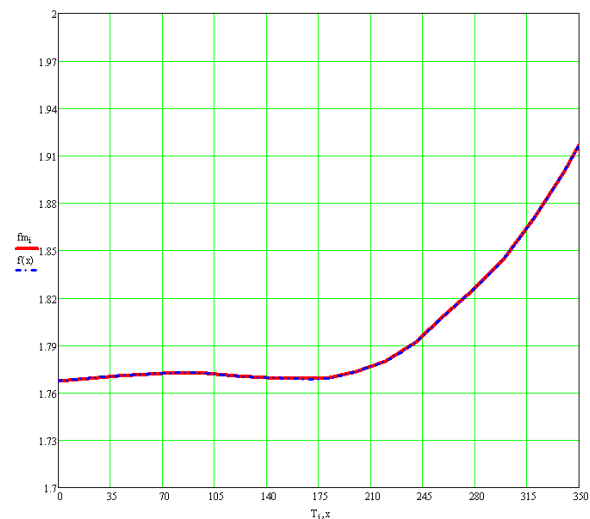


Figure 5 The variation of the material factor vs. the temperature

Having into account the experimental trials done with high speed trains shown in: [2, 3, 4, 12], it came out that at a brake stopping from the maximum speed, the train speed decreases approximate straight-line depending on time (brake time), thus, we can consider that the high speed train at a brake stopping performs an uniform deceleration motion, at which: $V = a \cdot t$, where a = deceleration (constant).

If the speed at the beginning of the brake stopping is $V = 200$ Km/h and brake time $t_b = 60$ s, using the Mathcad computer program, were calculated the coefficients of the approximation polynomial for the function $V = f(t)$ by the smallest squares method, and in figure 6 is represented this function using de cubic spline interpolation functions.

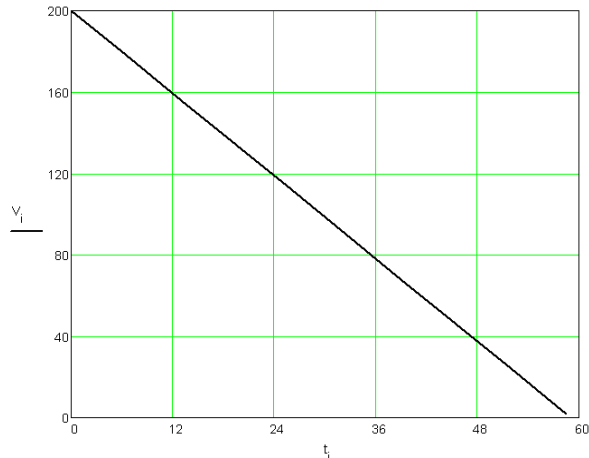


Figure 6. The variation of the circulation speed vs. the brake time

The brake space according with $V(t)$ variation is given by relation:

$$s_f = \frac{3,93 \cdot (1+\gamma) \cdot V^2(t)}{g \cdot \mu_s(t) \cdot \delta + rt} + \frac{V(t) \cdot tu}{7,2} \quad [\text{m}] \quad (4)$$

where: $(1+\gamma)$ = a factor which take into account the revolving masses of the vehicle (in calculation $1+\gamma = 1,05$);

g = gravity acceleration (it in calculation it is considered $g = 9,80665 \text{ m/s}^2$);

δ = brake coefficient (in calculation $\delta = 0,35$);

tu = time for filling the brake-cylinder with compressed air (in calculation $tu = 4 \text{ s}$);

rt = specific train resistance of the considered vehicle (in calculation $rt = 20 \text{ N/KN}$);

μ_s = friction coefficient between brake disk and friction pad (set).

For the determination of the brake space with relation (4) it was calculated with Karwatsky's formula, [13], the friction coefficient between brake disk and friction pad (set) for different pressure forces of the pad on the disk:

$$\mu_s(t) = 0,1177 \cdot \frac{F_b + 200}{F_b + 80} \cdot \frac{V(t) + 171,8}{V(t) + 105} \quad (5)$$

The values of the friction coefficient and of the brake space calculated for three different pressure forces ($F_b = 20 \text{ KN}$, $F_b = 45 \text{ KN}$ and $F_b = 50 \text{ KN}$) are presented in table 4.

Table 4 The values of the friction coefficient and of the brake space for different pressure forces of the friction pad (set) on the brake disk.

$F_b = 20 \text{ KN}$		
Speed V [Km / h]	Friction coefficient μ_s	Brake space Sr [m]
0	0,42214618	0
20	0,39603319	23,078
40	0,37712378	72,453
60	0,36279848	150,745
80	0,35157053	259,733
100	0,34253341	400,671
120	0,33510288	574,464
140	0,32888550	781,785
160	0,32360660	1023,144
180	0,31906859	1298,932
200	0,31512573	1609,457

$F_b = 45 \text{ KN}$		
Speed V [Km / h]	Friction coefficient μ_s	Brake space Sr [m]
0	0,37609387	0
20	0,35282957	24,519
40	0,33598301	78,498
60	0,32322046	164,867
80	0,31321738	285,613
100	0,30516612	442,138
120	0,29854620	635,453
140	0,29300708	866,309
160	0,28830406	1135,276
180	0,28426111	1442,791
200	0,28074838	1789,198

$F_b = 50 \text{ KN}$		
Speed V [Km / h]	Friction coefficient μ_s	Brake space Sr [m]
0	0,36900890	0
20	0,34618286	24,772
40	0,32965366	79,560
60	0,31713153	167,346
80	0,30731690	290,158
100	0,29941731	449,418
120	0,29299210	646,160
140	0,28748733	881,148
160	0,28287290	1154,961
180	0,27890611	1468,045
200	0,27545955	1820,749

Using the values calculated, in figures 7 and 8 are shown the variations of the friction coefficient depending on speed and the variation of the brake space depending on speed for the three pressure forces presented before:

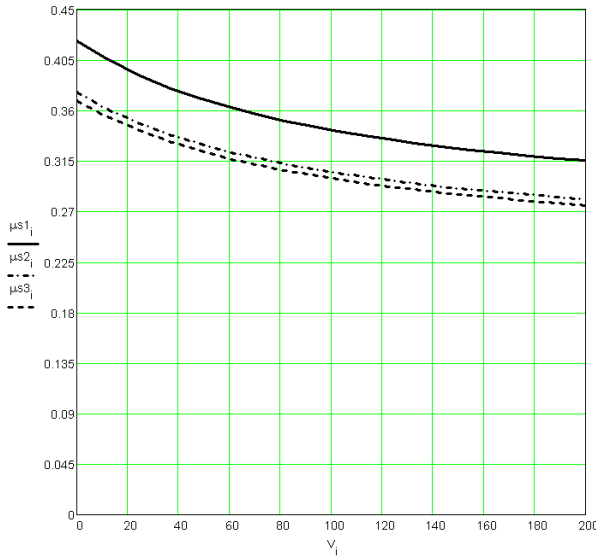


Figure 7. The variation of the friction coefficient between the brake disk and friction pad vs. the speed.

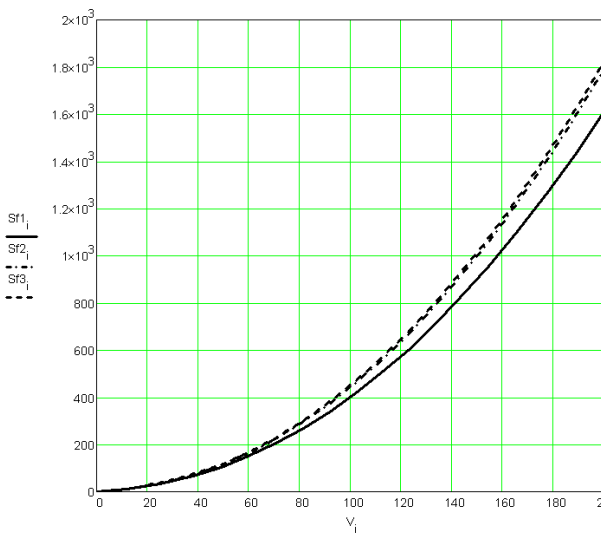


Figure 8. The variation of the brake space vs. the speed.

The decelerations which were used for getting these brake spaces, at a straight-line variation of the speed depending on time, are determined with relation:

$$a = \frac{\left(\frac{V(t)}{3,6}\right)^2}{2 \cdot Sf} \quad [m/s^2] \quad (6)$$

The deceleration values for the three pressure forces of the friction pad on the brake disk are presented in table 5.

Table 5. The deceleration values for the pressure forces

Speed V [Km / h]	Deceleration a [m / s ²]		
	F _b = 20 KN	F _b = 45 KN	F _b = 50 KN
0	0	0	0
20	0,668696	0,629382	0,62295
40	0,851978	0,78636	0,775866
60	0,921351	0,84243	0,829946
80	0,950643	0,864502	0,850962
100	0,962891	0,872583	0,858447
120	0,967085	0,874267	0,859779
140	0,962738	0,872867	0,858167
160	0,965314	0,869969	0,855141
180	0,962329	0,866377	0,851473
200	0,958839	0,862515	0,847569

Using the values from the table 5, in figure 9, are shown the brake decelerations for the three pressure forces of the brake pad (set) on the brake disk.

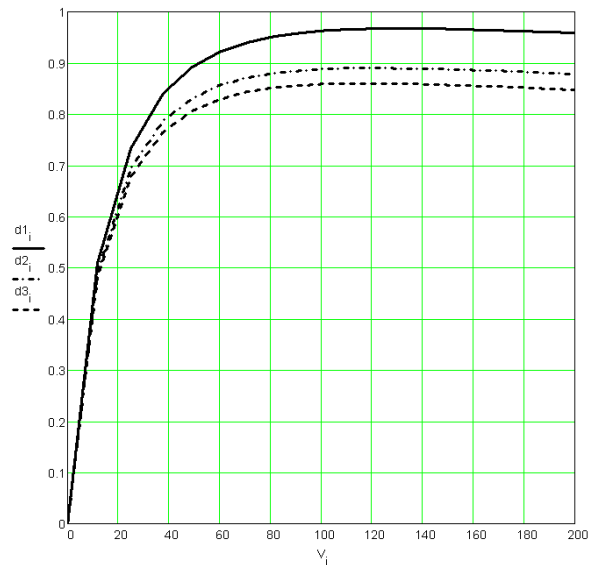


Figure 9. The variation of the brake deceleration vs. the speed

4. CONCLUSIONS

From the data analysis of the tables and diagrams presented in this work result the next conclusions:

- For the determination of the brake characteristics (friction coefficient between the friction coupling elements, brake space, brake deceleration) and of the brake disk and friction pad (set) friction surfaces average temperatures we must consider the variation

depending on temperature of the physical properties of the materials which are used for the brake disk and friction pad (in disk brake case: friction pad-brake disk);

- Having in to account the experimental trials done with high speed trains shown in specialty literature, [2, 3, 4, 12], it was found that at a brake stopping from a maximum speed, the trains speed decreases almost straight-line depending on time (brake time), thus, we can consider that the high speed train, at a brake stopping executes an uniform deceleration motion, at which $V = a \cdot t$ where $a =$ deceleration (constant);
- The material densities from which are manufactured the elements of the friction coupling (gray iron Fc 250, for disk and a **composite material** JURID 874 for friction pad) were considered constant with temperature range: 0 - 350° C, these vary insignificant with temperature;
- Using the values of the specific heat and of the thermal conductivity of the friction coupling material elements, for different temperatures, presented in specialty literature: [15-16], were determined the approximation polynomial coefficients for the functions: $c_g(T)$, $c_d(T)$, $\lambda_d = f(T)$ and $\lambda_g = f(T)$, using the smallest squares method, and the graphic representation of these variations was done by the cubic spline interpolation functions;
- Analyzing the diagrams from figures 1 and 2 we can observe a complete variation different with temperature of the specific heat for the two materials of the friction coupling elements (the increasing allure with temperature of the brake disk material specific heat and a decreasing allure of the friction pad material specific heat), having a large influence upon brake characteristics and of the thermal regime of the brake disk and friction coupling elements friction surface;
- Material factor f_m [10-12] considered constant with temperature was reconsidered

in this work, keeping in to account of the modification of the specific heat (c) and of the thermal conductivity (λ) depending on temperature (factor f_m is not constant any more with temperature but depending on this);

- We observe (see figure 8) that when we increase the pressure force of the friction pad on the brake disk, deceleration decrease (at 180 km/h and $F_b = 20$ kN, deceleration has $d = 0,962329$ m/s² value, and for $F_b = 45$ kN, deceleration decrease at $d = 0,866377$ m/s² value), situation which leads at a increasing of the brake space (from $S_f = 1298,932$ m to $S_f = 1442,791$ m) and to a thermal regime more “tolerable” for the elements of the friction coupling of the disk brake (friction pads and brake disk);
- Result, thus, the fact that the variation depending on temperature of the physical properties of the friction coupling material elements influences the brake characteristics of the disk brake, direct, by the friction coefficient obtained at certain speeds at the beginning of the brake, and, indirect, by the expression of this coefficient in the calculation relation of the brake space (for example: at a speed at the beginning of the brake of 200 km/h and a pressure force $F_b = 45$ kN, we obtain a friction coefficient $\mu_s = 0,28074838$, which decreases at de value of $\mu_s = 0,27545955$, at a bigger pressure force $F_b = 50$ kN, by cause of the high level for the temperature which is on the friction surface of the friction coupling elements of the disk brake).

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Determinarea caracteristicilor de frânare în cazul variației cu temperatura a proprietăților materialelor cuplei de frecare a frânei cu disc a vehiculelor feroviare

Rezumat

Siguranța circulației vehiculelor feroviare clasice și de mare viteză depinde de modul de funcționare și caracteristicile sistemelor de frânare ale acestora. Frânarea vehiculelor feroviare (în special frânarea de oprire) se poate face utilizând frâne din același sistem (de exemplu frâna cu saboți sau frâna cu disc din sistemul mecanic de frânare) sau combinând frâne din mai multe sisteme (frâna cu disc-

sistemul mecanic, frâna electromagnetică pe șină sau frâna electrică rezistivă sau recuperativă – sistemul electric de frânare). În timpul frânării de oprire elementele cuplei de frecare ale frânei principale – frâna cu disc, ating temperaturi destul de mari (în special la frânarea de la viteze mari $V > 160$ km/h) care conduc la alterarea proprietăților fizico-chimice și mecanice ale materialelor acestor elemente.

În această lucrare se prezintă caracteristicile de frânare ale vehiculelor feroviare (coeficientul de frecare, spațiul de frânare și decelerația la frânare) în cazul variației proprietăților fizice (caldura specifică și conductibilitate termică) ale materialelor elementelor cuplei de frecare ale frânei disc (disc de frână - plăcuță de frecare) cu temperatura.

Liviu Sevastian BOCÎI, Professor, PhD, "Aurel Vlaicu" University of Arad; Department of Automation, Industrial Engineering, Textiles and Transport; no 2, Elena Drăgoi Street, 310330 Arad, Romania, tel/fax: +40 257 250389; bociis@yahoo.com

Jacob Javier VASQUEZ SANJUAN, Professor, PhD. Polytechnic University of Puebla, Mexico, Automotive Systems Department, 727460 Puebla, Mexico, +52 222 774 665, Jacob.vasquez@up Puebla.edu.mx.