



TECHNICAL UNIVERSITY OF CLUJ-NAPOCA

ACTA TECHNICA NAPOCENSIS

Series: Applied Mathematics, Mechanics, and Engineering
Vol. 60, Issue III, September, 2017

STUDY OF CHANGING GEOMETRIC CHARACTERISTICS IN PROXIMAL FEMORAL BONE AFFECTED BY OSTEOPOROSIS IN COMPLIANCE WITH SINGH INDEX

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Abstract: The present study aims to analyze the geometric characteristics of four cross - sections (femoral head, femoral neck, intertrochanteric and diaphysis) from the proximal femoral bone area. Depending on the process of degradation of trabecular tissue generated by osteoporosis, a process characterized by the Singh index, the geometric characteristics of the cross – section were determined in different areas of the proximal femoral bone: area of shape, the coordinates of the center of gravity, moment of inertia, product of inertia, radius of gyration and static moments of surface.

Key words: proximal femoral bone, osteoporosis, trabecular tissue, cortical tissue, geometrical characteristics of cross section

1. INTRODUCTION

The present study aims to analyze the geometric characteristics of four cross - sections (femoral head - FH, femoral neck - FN, intertrochanteric - IT and diaphysis - D) from the proximal femoral bone (PFB) area, according to Figure 1.



Fig. 1. Femoral bone sectioned in the cross - section plane.

In the computational relations of stresses and deformations produced by axial loading (produced by the axial forces, N) or the shear loading (produced by the cutting forces, T), the cross – section (CS) of the proximal femoral bone (Fig.2), affected by osteoporosis (OP), occurs in its simplest form, namely by the value of its area of shape (AOS). For this cases of loading the CS geometry does not play any role.

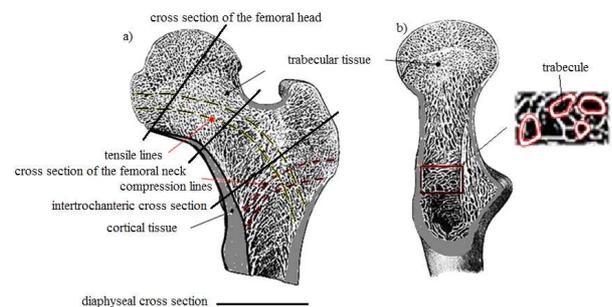


Fig. 2. The structure of PFB. a) longitudinal section; b) sagittal section.

In the study of the state of stresses and deformations caused by other simple loading, such as bending, torsion, or in the case of composite loading, geometric notions of a more complex form than the CS area occur. These are moments of varying degrees of CS, such as static moments of surface (SMOS) (moments of the first degree), moment of inertia (MOI) and polar moment of inertia (PMOI), product of inertia (POI), radius of gyration (ROG), section modulus (axial – SMA and polar SMP). Their values depend on both size and the shape of the CS studied.

Generally, in the technical literature, the term geometrical characteristics of the PFB relate to: hip axis length, inclination angle or flexion of FN, angle of declination of FN, D

dimensions (outer distance, inner distance), FN dimensions (outer distance, inner distance), FH dimensions (outer distance, inner distance), IT distance. All these dimensions are determined mainly by anteroposterior (AP) X-rays or scanning by computer tomography (CT) [1, 2, 3, 4, 5, 6, 7] but also with digital photography [8]. If reference is made to the geometric characteristics of the CS (AOS, SMOS, MOI, PMOI, POI, ROG, SMA, SMP) can be shown that the number of scientific works which meet the subject is relatively low [9, 10].

In order to determine the size of these parameters, it is necessary to know in depth the architectural microstructure of the trabecular tissue [11, 12, 13, 14, 15]. If the trabecular structure is affected by osteoporosis, using the Singh index and bone mineral density (BMD), its degradation may be highlighted [16, 17, 18].

It is assumed that the trabecular dimensions of the different trajectory groups (primary and secondary compression group, main and secondary stretch group) depend on the magnitude of the mechanical stress level of the human body and that when the BMD decreases trabecular pattern register a regression, in a predictable sequence. In 1970 M. Singh, A.R. Nagrath and P.S. Maini proposed a classification system based on this phenomenon by a comparative x-ray of the PFB radiograph showing OP with radiographies considered to be „normal”. This classification system is called Singh’s system. Under this system there are six degrees of visibility of the trabecular structure of the PFB, according to Figure 3. Grades 6 to 4 are considered normal and grades 3 to 1 indicate OP.

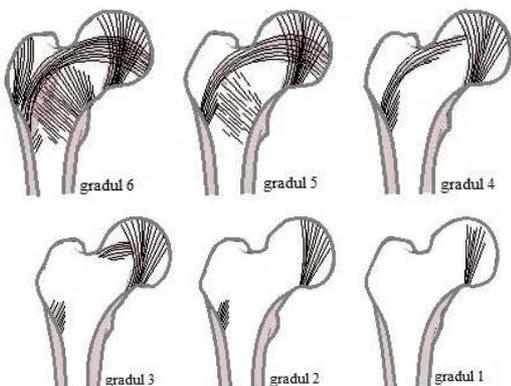


Fig. 3. Hierarchy of the Singh index.

Currently, BMD is the surrogate parameter of bone mass in OP. Osteodensitometry is the non-invasive method

that allows BMD measurement, and as long as the identification of the OP remains tributary to the quantitative element, it is the main method of diagnosing the disease in the preclinical stage, that is before the occurrence of the fractures. From the perspective of the OP’s particularities regarding the architecture of the trabecular structure of the PFB and the fact that it is affected by a gradual regression, the geometric characteristics of the four CS mentioned above (Fig.2) were determined.

2. METHODS

The femoral bone chosen for the study is estimated to be characteristic of an overweight person with a body mass index BMI=25.6. Following sectioning in the transverse plane of the PFB (Fig.1), the following four CS were taken into consideration: FH, FN, IT and D, according to Figure 4.

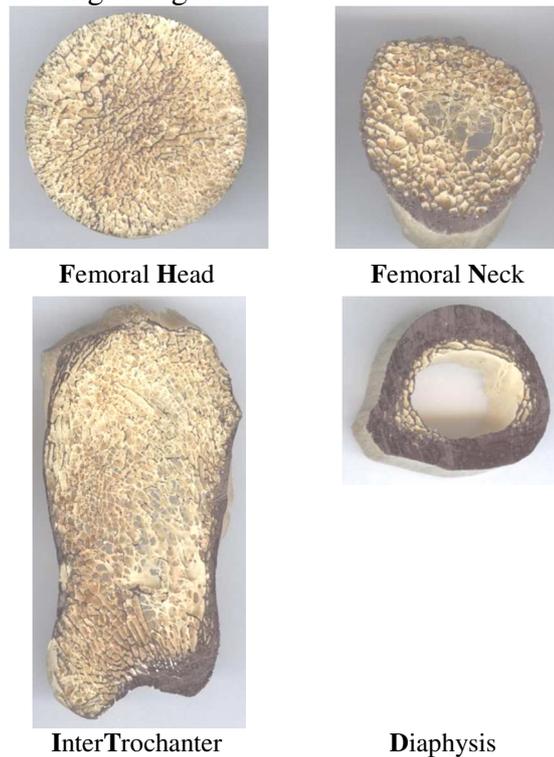


Fig. 4. Cross Sections considered.

To highlight the current sectional plane with respect to deep trabecular elements, a contrast paint was used. In the next step the four CS are scanned to obtain four files in .jpeg format. Thus, in the case of the CS of the FH area, the dimensions are 2,320x2,304 pixels and the horizontal and vertical resolution is 1,200 dpi, in the case of the CS in the FN area the

dimensions are 1,584x1,696 pixels and the horizontal and vertical resolution is 1,200 dpi, in the CS of the IT area the dimensions are 2,208x4,000 pixels and the horizontal and vertical resolution is 1,200 dpi, in the case of the CS of the D area the dimensions are 1,648x1,584 pixels and the horizontal and vertical resolution is 1,200 dpi. The next step is to highlight the structure of the cortical and trabecular tissue in the plane of interest by eliminating in-depth planes using an image editing software, as shown in Figure 5.

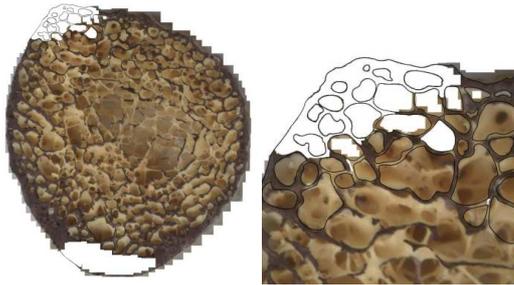


Fig. 5. Define the current plane for the CS of the FN.

The CS in the final form is shown in Figure 6.

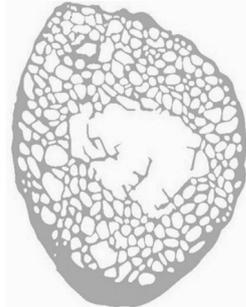


Fig. 6. The CS, in the final form, of the FN.

In the next step, the current surface is discretized through a number of nodes, according to Figure 7. For the FH section were needed 5,791 nodes, for the FN section were needed 3,500 nodes, for the IT section were needed 10,117 nodes, for the D section were needed 855 nodes, in total 20,263 nodes.

By scaling the image using Digimizer software, the position can be determined in the cartesian coordinate of each node.

Starting from such a configuration, considered to be the basic section, by introducing the cartesian coordinates in the AutoCad software, also taking into account the Singh index of degradation of the trabecular structure is obtained, according to Figure 8, Figure 9, Figure 10, Figure 11, 5 configurations for the FH section, 6 configurations for the FN

section, 6 configurations for the IT section and 5 configurations for the D section.

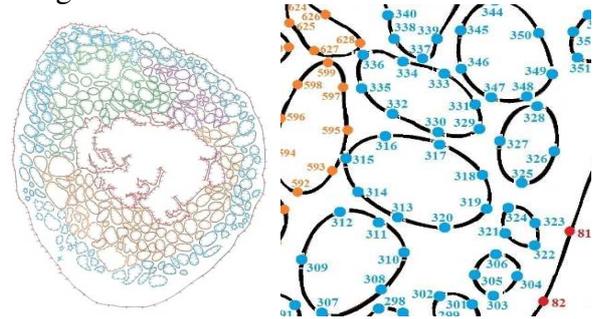


Fig. 7. Numbering nodes.

According to Figure 8, the CS of the FH considered healthy has a number of 904 traves. When the trabecular structure is affected by OP, for Grade 4 there are 690 traves with a deterioration percentage of 23.67 relative to the structure considered to be healthy; for Grade 3 there are 424 traves with a deterioration percentage of 53.09 compared to the structure considered to be healthy; for Grade 2 there are 114 traves with a deterioration percentage of 87.38 compared to the structure considered to be healthy and Grade 1 there are 27 traves with a 97.01 damage percentage compared to the structure considered to be healthy.

According to Figure 9, the CS of the FN considered healthy has a number of 392 traves. When the trabecular structure is affected by OP, for Grade 5 there are 258 traves with a deterioration percentage of 34.18 relative to the structure considered to be healthy; for Grade 4 there are 154 traves with a deterioration percentage of 60.71 compared to the structure considered to be healthy; for Grade 3 there are 2 traves with a deterioration percentage of 99.48 compared to the structure considered to be healthy; for Grade 2 and 1 there is no longer a travee recorded with a deterioration percentage of 100 compared to the structure considered to be healthy.

According to Figure 10, the CS of the IT considered healthy has a number of 1,712 traves. When the trabecular structure is affected by OP, for Grade 5 there are 1,229 traves with a deterioration percentage of 28.21 relative to the structure considered to be healthy; for Grade 4 there are 591 traves with a deterioration percentage of 65.47 compared to the structure considered to be healthy; for Grade 3 there are

256 traves with a deterioration percentage of 85.04 compared to the structure considered to be healthy; for Grade 2 there are 81 traves with a 95.26 damage percentage compared to the structure considered to be healthy and Grade 1 there are 20 traves with a 98.83 damage percentage compared to the structure considered to be healthy.

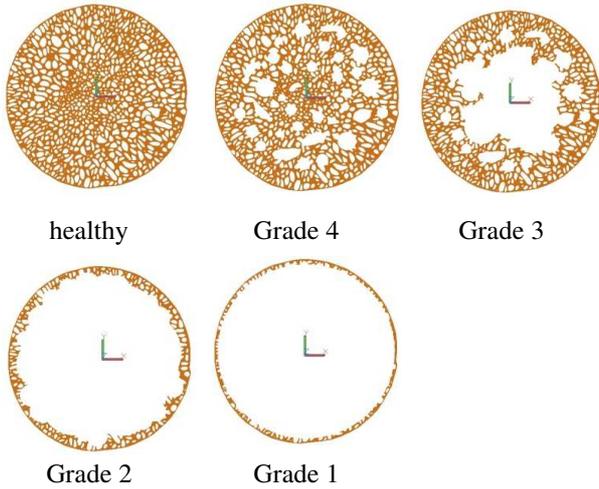


Fig. 8. The CS of the FH area.

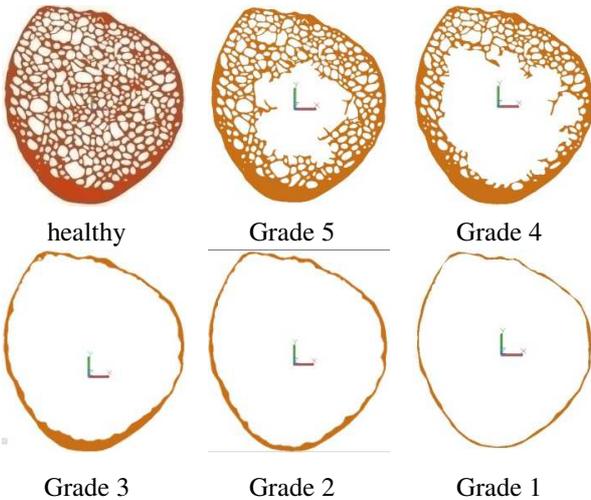


Fig. 9. The CS of the FN area.

According to Figure 11, the CS of the D considered healthy has a number of 78 traves. When the trabecular structure is affected by OP, for Grade 4 there are 37 traves with a deterioration percentage of 52.56 relative to the structure considered to be healthy; for Grade 3 there are 4 traves with a deterioration percentage of 94.87 compared to the structure considered to be healthy; for Grade 2 there are 1 trave with a deterioration percentage of 98.71 compared to the structure considered to be healthy and Grade 1 there is no longer a travee recorded with a

deterioration percentage of 100 compared to the structure considered to be healthy.

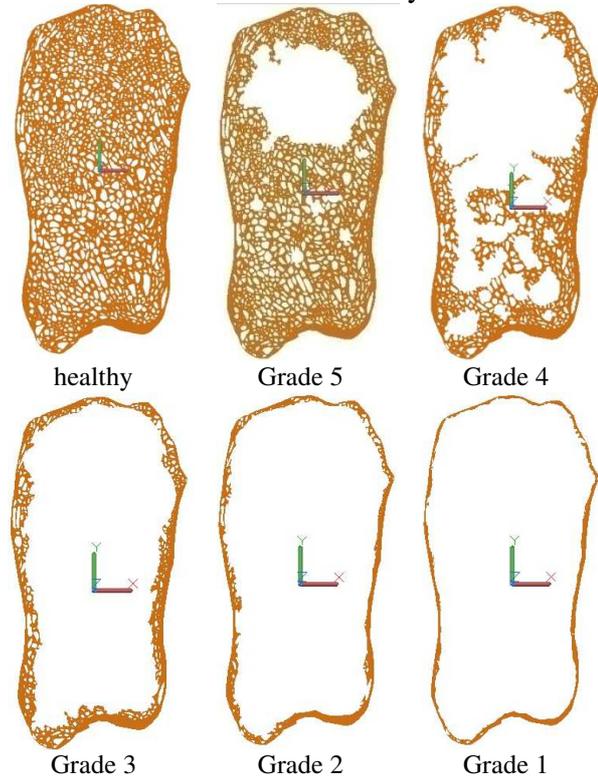


Fig. 10. The CS of the IT area.

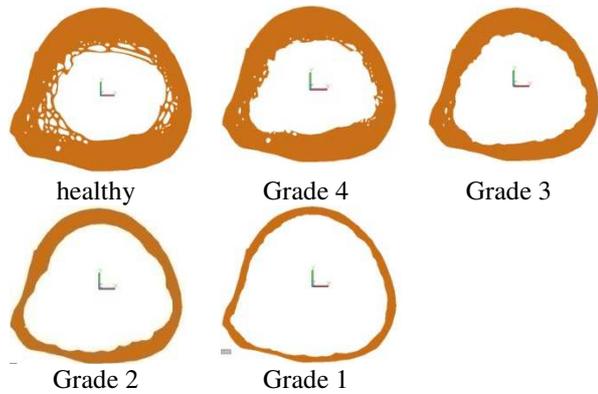


Fig. 11. The CS of the D area.

Analytically, it is admitted that the surface area A is composed of a number of surface elements with infinitely small size, of area dA . Is defined the SMOS (or moment of the first degree of surface) in relation to the axes Oz and Oy the sum of the products between the infinite small areas dA of the surface elements and the distances of these elements at the considered axis [19]. SMOS are measured in mm^3 , cm^3 etc.

$$S_z = \int_A y \cdot dA = y_c \cdot A \quad (1)$$

The coordinates of the center of gravity of the complex surface can be determined by the following relationship:

$$y_c = \frac{S_z}{A} = \frac{y_1 \cdot A_1 + y_2 \cdot A_2 + \dots + y_n \cdot A_n}{A_1 + A_2 + \dots + A_n} \quad (2)$$

$$z_c = \frac{S_y}{A} = \frac{z_1 \cdot A_1 + z_2 \cdot A_2 + \dots + z_n \cdot A_n}{A_1 + A_2 + \dots + A_n} \quad (3)$$

MOI and POI can be determined through Steiner's formulas:

$$I_z = \sum_{i=1}^n (I_{z_i} + y_{c_i}^2 A_i) \quad I_y = \sum_{i=1}^n (I_{y_i} + z_{c_i}^2 A_i) \quad (4)$$

$$I_{zy} = \sum_{i=1}^n (I_{z_i y_i} + y_{c_i} z_{c_i} A_i) \quad (5)$$

3. RESULTS

Once the geometries of the analyzed models are defined in the AutoCAD software, the MASSPROP command (according to Figure 12) generates the values for the following characteristics of the CS: moment of inertia (MOI) and polar moment of inertia (PMOI),

product of inertia (POI), radius of gyration (ROG), etc.

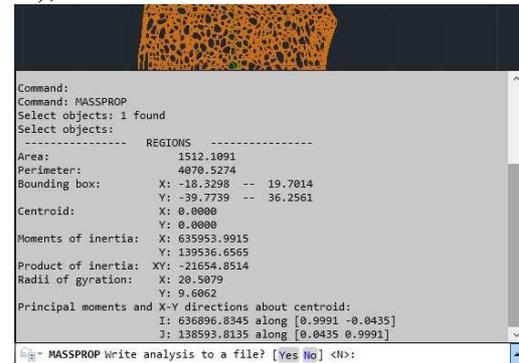


Fig. 12. The geometric characteristics generated in AutoCAD with the MASSPROP command.

Thus, in Table 1 the geometric characteristics of the CS of the FH area are centralized; in Table 2 the geometric characteristics of the CS of the FN area are centralized; in Table 3 the geometric characteristics of the CS of the IT area are centralized and in Table 4 the geometric characteristics of the CS of the D area are centralized.

Table 1

Geometric characteristics of the CS of the FH area.

Femoral Head - FH												
	health		Gr.5		Gr.4		Gr.3		Gr.2		Gr.1	
traves	904		904		690		424		114		27	
Area[mm ²]	821.5		821.5		697.7		492.3		164.4		82.6	
Bounding box												
z[mm]	20.8	20.9	20.8	20.9	20.7	21.0	20.6	21.1	21.6	20.1	20.6	21.1
x[mm]	21.3	21.4	21.3	21.4	21.3	21.4	21.1	21.6	21.2	21.5	20.5	22.2
Moments of Inertia – MOI and POI												
I _z [mm ⁴] x10 ⁴	9.4		9.4		8.4		7.7		3.3		1.8	
I _x [mm ⁴] x10 ⁴	9.01		9.01		8.06		7.3		3.2		1.6	
I _{zx} [mm ⁴]	-2,479.6		-2,479.6		-829.7		-876.5		-874.03		-492.5	
Radius of gyration - ROG												
r _z [mm]	10.7		10.7		11.0		12.5		14.3		15.09	
r _x [mm]	10.4		10.4		10.7		12.2		14.1		14.2	
The upper half												
Area[mm ²]	407.9		407.9		345.7		241.7		82.4		39.6	
x _c [mm]	9.1		9.1		9.4		11.3		12.8		14.2	
S _z [mm ³]	3,737.3		3,737.3		3,252.7		2,745.7		1,060.5		566.2	
The lower half												
Area[mm ²]	413.6		413.6		351.9		250.6		82.06		43.0	
x _c [mm]	-9.03		-9.03		-9.2		-10.9		-12.9		-13.1	
S _z [mm ³]	3,737.1		3,737.1		3,252.5		2,745.6		1,060.4		566.2	

Table 2

Geometric characteristics of the CS of the FN area.												
Femoral Neck - FN												
	health		Gr.5		Gr.4		Gr.3		Gr.2		Gr.1	
traves	392		258		154		2		0		0	
Area[mm ²]	319.4		255.6		191.4		63.2		47.4		27.4	
Bounding box												
z[mm]	13.1	13.8	12.9	14.05	12.6	14.3	12.7	14.2	12.9	14.02	13.05	13.8
x[mm]	14.4	15.8	14.5	15.7	14.9	15.3	11.3	15.9	13.2	17.09	14.4	15.8
Moments of Inertia – MOI and POI												
I _z [mm ⁴] $\times 10^4$	2.02		1.9		1.6		0.6		0.4		0.2	
I _x [mm ⁴] $\times 10^4$	1.6		1.5		1.2		0.4		0.3		0.2	
I _{zx} [mm ⁴]	486.6		529.2		-81.7		83.08		-6.2		193.8	
Radius of gyration - ROG												
r _z [mm]	7.9		8.6		9.3		10.2		10.09		9.8	
r _x [mm]	7.08		7.6		8.1		8.3		9.1		9.7	
The upper half												
Area[mm ²]	158.2		127.4		98.8		26.1		22.1		13.1	
x _c [mm]	6.8		7.6		8.1		11.07		9.6		9.05	
S _z [mm ³]	1,077.8		980.3		807.4		289.8		213.1		119.064	
The lower half												
Area[mm ²]	161.1		128.1		92.6		37.04		25.2		14.3	
x _c [mm]	-6.6		-7.6		-8.7		-7.8		-8.4		-8.3	
S _z [mm ³]	1,077.8		980.4		807.4		289.8		213.09		119.07	

Table 3

Geometric characteristics of the CS of the IT area.												
InterTrochanteric - IT												
	health		Gr.5		Gr.4		Gr.3		Gr.2		Gr.1	
traves	1,712		1,229		591		256		81		20	
Area[mm ²]	1,512.1		1,208.2		746.05		388.8		227.7		147.1	
Bounding box												
z[mm]	18.3	19.7	18.2	19.7	18.9	19.07	18.0	20.02	17.6	20.3	19.2	18.7
x[mm]	39.7	36.2	35.7	40.2	32.6	43.4	34.2	41.7	35.05	40.9	34.9	41.04
Moments of Inertia – MOI and POI												
I _z [mm ⁴] $\times 10^4$	63.5		51.7		34.5		22.2		14.3		8.7	
I _x [mm ⁴] $\times 10^4$	13.9		12.6		9.3		6.7		4.2		2.8	
I _{zx} [mm ⁴]	-21,654.8		-21,892.8		-15,124.5		-8,020.3		-4,965.4		-3,655.9	
Radius of gyration - ROG												
r _z [mm]	20.5		20.6		21.5		23.9		25.1		24.4	
r _x [mm]	9.6		10.2		11.1		13.1		13.5		13.8	
The upper half												
Area[mm ²]	781.3		579.2		321.1		185.7		109.02		71.4	
x _c [mm]	17.1		18.2		20.9		22.06		23.3		22.1	
S _z [mm ³]	13,411.5		10,559.2		6,712.5		4,098.6		2,546.1		1,585.08	
The lower half												
Area[mm ²]	730.8		628.9		424.8		203.1		118.7		75.6	
x _c [mm]	-18.3		-16.7		-15.7		-20.1		-21.4		-20.9	
S _z [mm ³]	13,411.4		10,559.3		6,712.7		4,098.6		2,545.9		1,585.01	

Table 4

Geometric characteristics of the CS of the D area.												
Diaphysis												
	health		Gr.5		Gr.4		Gr.3		Gr.2		Gr.1	
traves	78		78		37		4		1		0	
Area[mm ²]	294.5		294.5		265.1		206.4		147.2		88.3	
Bounding box												
z[mm]	13.4	13.4	13.4	13.4	13.6	13.2	13.3	13.4	13.9	12.9	13.9	12.9
y[mm]	11.2	13.05	11.2	13.05	11.2	12.9	11.8	12.4	11.7	12.5	11.8	12.3
Moments of Inertia – MOI and POI												
I _z [mm ⁴] x10 ⁴	1.6		1.6		1.5		1.2		0.9		0.5	
I _y [mm ⁴] x10 ⁴	1.6		1.6		1.5		1.2		0.9		0.6	
I _{zy} [mm ⁴]	-130.7		-130.7		188.8		-5.5		524.6		94.3	
Radius of gyration - ROG												
r _z [mm]	7.5		7.5		7.5		7.8		8.1		8.2	
r _y [mm]	7.4		7.4		7.5		7.8		8.1		8.8	
The upper half												
Area[mm ²]	144.2		144.2		131.8		102.3		75.05		44.3	
z _c [mm]	6.6		6.6		6.6		7.0		7.12		7.9	
S _y [mm ³]	961.7		961.7		874.7		717.5		534.5		350.9	
The lower half												
Area[mm ²]	150.2		150.2		133.3		104.0		72.2		43.9	
z _c [mm]	-6.5		-6.5		-6.5		-6.8		-7.3		-7.9	
S _y [mm ³]	959.5		959.5		874.6		717.6		534.4		350.8	

4. CONCLUSIONS

Depending on the process of degradation of the trabecular tissue generated by osteoporosis, a process characterized by the Singh index, the geometric characteristics of the cross - section were determined in different areas of the proximal femoral bone: area of shape, the coordinates of the center of gravity, moment of inertia, product of inertia, radius of gyration and static moments of surface.

These geometric characteristics of cross – section play an important role in determining the stress and deformation state as well as the buckling stability of the proximal femoral bone.

From the results it can be pointed out that the area of shape, moment of inertia, product of inertia and static moments of surface registers a progressive regression with the evolution of osteoporosis, this signifying a weakening of the resistance in the proximal femoral bone area.

5. ACKNOWLEDGEMENTS

This study was made possible by the technical support given by Curean Rareş, Duma Irina and Filipovici Dumitreasa Emil, students at the Automotive Engineering and

Transportations Department, Faculty of Mechanics, Technical University of Cluj Napoca, Romania.

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Studiul modificării caracteristicilor geometrice în osul femural proximal afectat de osteoporoză, în concordanță cu indicele Singh

Rezumat: Prezentul studiu își propune analiza caracteristicilor geometrice a patru secțiuni transversale (cap femural, col femural, intertrohanteric și diafiză) din zona osului femural proximal. În funcție de procesul de degradare a țesutului trabecular generat de către osteoporoză, proces caracterizat prin intermediul indicelui Singh, în diferitele zone ale femurului proximal s-au determinat caracteristicile geometrice ale secțiunii transversale: aria A, perimetrul, coordonatele centrului de greutate, momentele de inerție axiale, momentul de inerție centrifugal, razele de rotație (razele minime de inerție) precum și momentul static.

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