STABILITY OF HUMAN BODY SUBJECTED TO VIBRATIONS ON A VIBRATING PLATE

Mariana ARGHIR

Abstract: The paper presents a study of the stability of the human body, subjected to vibrations on a vibrating platform. The body of a human operator, subject to study is placed inclined on the vibrating plate, which runs in vertical vibrations, with constant frequency. The body is divided into six distinct segments, for which we know the mechanical characteristics, as determined by previous studies and for which it has been studied the dynamics of individual and of entire system. Through this paper seeks to analyse the stability of each segment of the body and bring their contribution to the analysis of vibration imposed on human organism in vibrational environment.

Key words: stability of human body, general vibrations on the vibrating platform, constant frequency.

1. INTRODUCTION

It is considered a human subject placed on a vibrating platform, which produces vertical vibrations. The body is placed at 45 ° inclined towards horizontal plate. A suggestive image can be date as in figure 1 [1].

In the Figure 1 are presented the gravity forces for the body segments (G_i, i=1 to 6), the action force (F(t)), that acts over the body situated on the vibrating platform, and the linkage forces (N_1 and N_2) the normal reactions on the segments who are posted assumed horizontal on the platform.

An important fact is that the action force is situated at the distance “l” about the application gravity force for the “4” segment, because here there is vertical direction of the mass centre position of the mechanical system. But the action force is divided into two different components, because they are direct applied on the subjected components of the human body. F_1(t) acts on the segment “1”, and F_2(t) component of the active force acts on the “4” segment.

This work is the continuation of the work [1] in which were established the differential equations of dynamics of material system assimilated human body posted on a horizontal vibrating platform.

System integration of differential equations, in order to establish the laws of motion of the material is done with Runge-Kutta method of order as well as 4 and a half, with variable pitch, Matlab programming environment.
2. DIFFERENTIAL EQUATIONS OF THE HUMAN BODY ON THE VIBRATING PLATFORM

Using the system (12) of differential equations [1], that govern the biomechanical system assimilated with the human body subjected to vibrations on the horizontal vibrating plate, they need to be transformed into a new system of differential equations having the second time derivative of the unknown quantity expressed over all unknown as in following relations. All the mechanical characteristics will be presented in the next paragraph of this paper.

2.1. Dorsal Region Leg

The dorsal region leg (foot) has only one unknown, because the segment “1”, it is considered that vertically vibrates only. The differential equation is given in the relation (1).

\[
\ddot{z}_1 = \frac{1}{m_1} \left[ F(t) - (c_{1v} + c_{2v}) \dot{z}_1 + c_{2v} \ddot{z}_1 \right] - (k_{1v} + k_{2v}) z_1 + k_{2v} z_2
\]

(1)

2.2. Crurale Region of the Previous Leg

The crurale region of the previous leg named and “calf of the leg” has two differential equations due to its inclined position reported to the vibrating platform. They are “z_2” for the vertical motion, and “x_2” for the horizontal motion.

\[
\ddot{z}_2 = \frac{1}{m_2} \left[ c_{2v} \dot{z}_1 + k_{2v} z_1 - \left( c_{2v} + \frac{\sqrt{2}}{2} (c_{3v} + c_{3h}) \right) \ddot{z}_2 + \left[ k_{2v} + \frac{\sqrt{2}}{2} (k_{3v} + k_{3h}) \right] z_2 + \right. \\
\left. + \frac{\sqrt{2}}{2} (c_{3v} + c_{3h}) \dot{z}_3 \right] + \frac{\sqrt{2}}{2} (k_{3v} + k_{3h}) z_3
\]

\[
\ddot{x}_2 = \frac{1}{m_2} \left[ \frac{\sqrt{2}}{2} (c_{3v} - c_{3h}) \dot{x}_3 + \frac{\sqrt{2}}{2} (k_{3v} - k_{3h}) x_3 \right] - \frac{\sqrt{2}}{2} (c_{3v} - c_{3h}) \ddot{x}_2 - \frac{\sqrt{2}}{2} (k_{3v} - k_{3h}) x_2
\]

(2)

2.3. Femoral Region Leg

The femoral region leg (femur) has two differential equations due to its inclined position. The unknown are “z_3” for the vertical motion, and “x_3” for the horizontal one.

\[
\ddot{z}_3 = \frac{1}{m_3} \left[ \sqrt{2} \left( c_{3v} + c_{3h} \right) \ddot{z}_2 + \frac{\sqrt{2}}{2} (k_{3v} + k_{3h}) \dot{z}_2 - \frac{\sqrt{2}}{2} (c_{3v} + c_{3h} + c_{4v} + c_{4h}) \ddot{z}_5 - \frac{\sqrt{2}}{2} (k_{3v} + k_{3h} + k_{4v} + k_{4h}) z_5 + \right. \\
\left. + \frac{\sqrt{2}}{2} (c_{4v} + c_{4h}) \dot{z}_4 + \frac{\sqrt{2}}{2} (k_{4v} + k_{4h}) z_4 \right] \\
\ddot{x}_3 = \frac{1}{m_3} \left[ \frac{\sqrt{2}}{2} (c_{4v} - c_{4h}) \dot{x}_5 + \frac{\sqrt{2}}{2} (k_{4v} - k_{4h}) x_5 \right] - \frac{\sqrt{2}}{2} (c_{4v} - c_{4h}) \ddot{x}_3 - \frac{\sqrt{2}}{2} (k_{4v} - k_{4h}) x_3
\]

(4)

2.4. Leg Buttocks Region

The leg buttocks region is posted in the horizontal position, but, due to the linkages with the neighboring segments, which are pitched at 45°, the motion is considered to be in both directions. The system of differential equations for this segment follows.

\[
\ddot{z}_4 = \frac{1}{m_4} \left[ F_2(t) + \frac{\sqrt{2}}{2} (c_{4v} + c_{4h}) \ddot{z}_3 + \frac{\sqrt{2}}{2} (k_{4v} + k_{4h}) z_3 - \frac{\sqrt{2}}{2} (c_{4v} + c_{4h} + c_{6v} + c_{6h}) \ddot{z}_5 - \frac{\sqrt{2}}{2} (k_{4v} + k_{4h} + k_{6v} + k_{6h}) z_5 + \right. \\
\left. + \frac{\sqrt{2}}{2} (c_{6v} + c_{6h}) \dot{z}_5 + \frac{\sqrt{2}}{2} (k_{6v} + k_{6h}) z_5 \right] \\
\ddot{x}_4 = \frac{1}{m_4} \left[ \frac{\sqrt{2}}{2} (c_{6v} - c_{6h}) \dot{x}_5 + \frac{\sqrt{2}}{2} (k_{6v} - k_{6h}) x_5 \right] - \frac{\sqrt{2}}{2} (c_{6v} - c_{6h}) \ddot{x}_4 - \frac{\sqrt{2}}{2} (k_{6v} - k_{6h}) x_4
\]

(6)
2.5. Abdominal Region

The abdomen is considered in this study as the “S” segment of the human body, and its motions and its stability can be obtained with two variable “z5” and “x5”, as follows.

\[
\ddot{z}_5 = \frac{1}{m_5} \left[ \frac{\sqrt{2}}{2} (c_{6V} + c_{6H}) \dot{z}_4 + \frac{\sqrt{2}}{2} (k_{6V} + k_{6H}) z_4 - \frac{\sqrt{2}}{2} (c_{6V} + c_{6H} + c_{7V} + c_{7H}) \dot{z}_5 - \frac{\sqrt{2}}{2} (k_{6V} + k_{6H} + k_{7V} + k_{7H}) z_5 + \frac{\sqrt{2}}{2} (c_{7V} + c_{7H}) \dot{z}_6 + \frac{\sqrt{2}}{2} (k_{7V} + k_{7H}) z_6 \right]
\]

(8)

\[
\ddot{x}_5 = \frac{1}{m_5} \left[ \frac{\sqrt{2}}{2} (c_{6V} - c_{6H}) \dot{x}_4 + \frac{\sqrt{2}}{2} (k_{6V} - k_{6H}) x_4 - \frac{\sqrt{2}}{2} (c_{6V} - c_{6H} + c_{7V} - c_{7H}) \dot{x}_5 - \frac{\sqrt{2}}{2} (k_{6V} - k_{6H} + k_{7V} - k_{7H}) x_5 + \frac{\sqrt{2}}{2} (c_{7V} - c_{7H}) \dot{x}_6 + \frac{\sqrt{2}}{2} (k_{7V} - k_{7H}) x_6 \right]
\]

(9)

2.6. Thorax Region

The thorax is the last part in our study, that has possibility to move into two perpendicular directions in the space under the action of the vibrations given by the vibrating platform. The scalar differential equations are for the two variables “z6” and “x6”.

\[
\ddot{z}_6 = \frac{1}{m_6} \left[ \frac{\sqrt{2}}{2} (c_{7V} + c_{7H}) \dot{z}_5 + \frac{\sqrt{2}}{2} (k_{7V} + k_{7H}) z_5 - \frac{\sqrt{2}}{2} (c_{7V} + c_{7H}) \dot{z}_6 - \frac{\sqrt{2}}{2} (c_{7V} + c_{7H}) z_6 \right]
\]

(10)

\[
\ddot{x}_6 = \frac{1}{m_6} \left[ \frac{\sqrt{2}}{2} (c_{7V} - c_{7H}) \dot{x}_5 + \frac{\sqrt{2}}{2} (k_{7V} - k_{7H}) x_5 - \frac{\sqrt{2}}{2} (c_{7V} - c_{7H}) \dot{x}_6 - \frac{\sqrt{2}}{2} (c_{7V} - c_{7H}) x_6 \right]
\]

(11)

3. MECHANICAL CHARACTERISTICS

Each segment is considered formed with: mass, spring, and damper. But, segments are considered with ideal characteristics. The mass does not have any elasticity, and damping. The spring has only elasticity, it does not have mass and capacity of depreciation, and the damper does not have mass and elasticity.

Me and my PhD student Vescan [2], we made together the mechanical characteristics for the segments presented above, and in this paper will be noted only the results. The masses will be given in Table 1, the segment elasticities can be taken from the Table 2, and the damper characteristics will find in the Table 3.

Table 1.

<table>
<thead>
<tr>
<th>Segment</th>
<th>Mass [kg]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Dorsal Region Leg</td>
<td>1.310</td>
</tr>
<tr>
<td>Shank</td>
<td>4.185</td>
</tr>
<tr>
<td>Femur</td>
<td>9</td>
</tr>
<tr>
<td>Gluteal region</td>
<td>12.780</td>
</tr>
<tr>
<td>Abdomen</td>
<td>12.510</td>
</tr>
<tr>
<td>Thorax</td>
<td>19.440</td>
</tr>
</tbody>
</table>

Table 2.

<table>
<thead>
<tr>
<th>Segment</th>
<th>Elastic Constant [N/m]</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>On second axis</td>
</tr>
<tr>
<td>Foot</td>
<td>1.777 x 10^5</td>
</tr>
<tr>
<td>Shank</td>
<td>0.403 x 10^5</td>
</tr>
<tr>
<td>Femur</td>
<td>0.473 x 10^5</td>
</tr>
<tr>
<td>Gluteal region</td>
<td>7.314 x 10^5</td>
</tr>
<tr>
<td>Abdomen</td>
<td>2.125 x 10^5</td>
</tr>
<tr>
<td>Thorax</td>
<td>1.751 x 10^5</td>
</tr>
</tbody>
</table>

Table 3.

<table>
<thead>
<tr>
<th>Segment</th>
<th>Damping Constant [Ns/m]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Foot</td>
<td>169.383</td>
</tr>
<tr>
<td>Shank</td>
<td>158.274</td>
</tr>
<tr>
<td>Femur</td>
<td>576.850</td>
</tr>
<tr>
<td>Gluteal region</td>
<td>16.571</td>
</tr>
<tr>
<td>Abdomen</td>
<td>65.314</td>
</tr>
<tr>
<td>Thorax</td>
<td>39.930</td>
</tr>
</tbody>
</table>

4. BIODYNAMIC SYSTEM STABILITY
Biodynamic system assimilated human body subjected to vibrations on a vibrating platform, is represented in the system of ordinal differential equations, nonhomogeneous, with constant coefficients, consisting of relationships (1) to (11).

The study was done on the two different directions of motion propagation. The vertical direction is given by the “z”, and the horizontal direction along the platform and parallel to it is the "x" coordinate.

4.1. VERTICAL STABILITY

4.1.1. Dorsal Region Leg

The (1) differential equation of the dorsal region leg (foot) was made with Runge-Kutta method. The Matlab representation is situated in the Figure 2, and its stability is given in the Figure 3.

4.1.2. Crurale Region of the Previous Leg

The (2) differential equation of the crurale region leg (shank) was made with Runge-Kutta method. The Matlab representation is situated in the Figure 4, and its stability is given in the Figure 5.

4.1.3. Femoral Region Leg

The femoral region leg (femur) will be presented in the Figure 6 with Runge-Kutta method integration for its differential equation of vertical displacement, and its stability in Matlab programming environment for the m₃ mass realises the Figure 7. They characterise the vertical motion of the femur in the dorsal leg, as in the relation (4).
4.1.4. Leg Buttocks Region

The buttocks leg has the Matlab representation in the figure 8, and its stability is given in the figure 9.

4.1.5. Abdomen

The (8) differential equation of the abdomen was made the Matlab representation in situated in the Figure 10, and its stability is given in the Figure 11.
4.1.6. Thorax

The thorax is last segment in this study, and it has the dynamics equation (10) for the vertical displacement. Its integration is given in the Figure 12, and the stability in the Figure 13.

![Fig. 12. The Matlab representation for the m₆ thorax](image)

**Vertical motion**

![Fig. 13. The m₆ thorax mass stability](image)

4.2. HORIZONTAL STABILITY

In the horizontal direction was made one representation in Matlab programming environment, for each coordinate of the biomechanical system assimilated with the human body.

![Fig. 14. The Matlab assembly for horizontally displacement of biomechanical system assimilated to the human body](image)
But, for better management of work space, is assembling the five representations in one (Fig. 14) for the entire system.

### 4.2.1. Crurale Region of the Previous Leg

The (3) differential equation of the crurale region leg (shank) was made with Runge-Kutta method. The Matlab representation is situated in the Figure 14 for the horizontal direction, and its stability is in the Figure 15.

![Fig. 15. The horizontal stability of the m₁ mass of the shank](image)

### 4.2.2. Femoral Region Leg

The femoral region leg (femur) will be presented in the Figure 14 with Runge-Kutta method integration for its differential equation of horizontal displacement, and its stability in Matlab programming environment for the m₃ mass realises the Figure 16. It characterises the horizontal motion of the femur in the dorsal leg, as in the relation (5).

![Fig. 16. The horizontal stability of the m₃ mass of the femur](image)

### 4.2.3. Leg Buttocks Region

The femoral region leg (femur) will be presented in the Figure 14 with Runge-Kutta method integration for its differential equation of horizontal displacement, and its stability in Matlab programming environment for the m₃ mass realises the Figure 17. It characterises the horizontal motion of the buttocks in the dorsal leg, as in the relation (7).

![Fig. 17. The horizontal stability of the buttocks m₄ mass](image)

### 4.2.4. Abdomen

The (9) differential equation of the abdomen was made the Matlab representation is situated in the Figure 14, and its horizontal stability is given in the Figure 18.

### 4.2.5. Thorax

The thorax is last segment in this study, and it has the dynamics equation (11) for the horizontal displacement. Its integration is given in the Figure 14, and the horizontal stability is situated in the Figure 19.
5. CONCLUSIONS

In this work it is proposed a new biomechanical model of human body subjected to connections on a vibrating platform. The human body is divided into six different segments of it, and it sat in an inclined position towards the platform with 45 degrees. Two segments are situated on the platform (foot and buttocks), and over them acts the active force having the distribution about them taking into account the masses of the segments.

Biomechanical system assimilated to the human body subjected to vibrations on a vibrating platform is a stable system. The platform makes the vertical vibrations with constant frequency of 30 Hz, and with an oscillation magnitude equal with 0.003m. The study was conducted on two directions of propagation of vibrations.

- Direction is vertical, so that the normal fluctuations of the platform are vertical. Depiction of the masses can be found in figures 3, 5, 7, 9, 11, 13. The vertical movement is stable for the human body.
- Direction of horizontal excitation arising from the tilt of the body segments. Movement is stable, as the result of the figures 15, 16, 17, 18, and 19.

6. BIBLIOGRAPHY


Stabilitatea corpului uman supus la vibratii pe o placa vibratoare

Rezumat: Lucrarea prezinta un studiu al stabilitatii corpului uman, supus la vibratii pe o platforma vibratoare. Corpul operatorului uman, supus studiului este asezat inclinat pe placa vibratoare, care executa vibratii verticale, cu frecventa constanta. Corpul este divizat in sase segmente distincte, pentru care se cunosc caracteristicile mecanice, stabilite prin studii anterioare si pentru care s-a studiat dinamica individului si a ntrezului sistem. Prin aceasta lucrare se caut a sa se analizeze stabilitatea fiecarii segment al corpului si isi aduce contributia la anliza vibratiilor impuse organismului uman in mediul vibrational.

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